Edexcel

A Level

A Level Maths

Edexcel Core Maths C1 June 2011 Model Solutions

Name:

M M E

Mathsmadeeasy.co.uk

Total Marks:

Edexcel C1   June 2011

1a. $25^{1/2} = \sqrt{25}$

$= 5$

1b. $25^{-3/2} = \dfrac{1}{25^{3/2}} = \dfrac{1}{(\sqrt{25})^3} = \dfrac{1}{125}$

2a. $y = 2x^5 + 7 + \dfrac{1}{x^3}$

$\dfrac{dy}{dx} = 10x^4 - 3x^{-4}$

2b. $\displaystyle\int 2x^5 + 7 + \dfrac{1}{x^3} \ dx$

$= \dfrac{2}{6}x^6 + 7x + \dfrac{x^{-2}}{(-2)} + c$

$= \dfrac{1}{3}x^6 + 7x - \dfrac{1}{2x^2} + c$

3. $P\ (-1,6)$ $Q\ (9,0)$

grad of PQ $= \dfrac{6-0}{-1-9} = \dfrac{6}{-10} = -\dfrac{3}{5}$

Mid of PQ $= \left(\dfrac{-1+9}{2}, \dfrac{6+0}{2} \right) = (4,3)$

L is $\perp$ $\therefore$ grad of L $= \dfrac{5}{3}$

$y - 3 = \dfrac{5}{3}(x-4)$

$3y - 9 = 5x - 20$

$5x - 3y - 11 = 0$

4.

$x + y = 2 \implies x = 2 - y$ ①

$4y^2 + -x^2 = 11$ ②

Sub ① into ②

$4y^2 - (2-y)^2 = 11$

$4y^2 - (4 - 4y + y^2) = 11$

$4y^2 - 4 + 4y - y^2 = 11$

$3y^2 + 4y - 15 = 0$

$(3y - 5)(y + 3) = 0$

$y = 5/3$ or -3

when $y = 5/3$; $x = 2 - 5/3$

$\qquad\qquad\qquad = 1/3$

$y = -3$; $x = 2 - (-3)$

$\qquad\qquad\qquad = 5$

5a.

$a_{n+1} = 5a_n + 3 \qquad a_1 = k$

$a_2 = 5a_1 + 3$

$\quad = 5k + 3$

5b.

$a_3 = 5a_2 + 3$

$\quad = 5(5k+3) + 3$

$\quad = 25k + 18$

5ci.

$\displaystyle\sum_{r=1}^{4} a_r = a_1 + a_2 + a_3 + a_4$

$a_4 = 5a_3 + 3$

$\quad = 5(25k + 18) + 3$

$\quad = 125k + 93$

$\displaystyle\sum_{r=1}^{4} a_r = k + 5k + 3 + 25k + 18 + 125k + 93$

$\quad = 156k + 114$

5ci. $\sum_{r=1}^{4} a_r = 6(26k + 19)$

$\therefore$ a multiple of 6

6a. $\dfrac{6x + 3x^{5/2}}{\sqrt{x}} = \dfrac{x^{1/2}(6x^{1/2} + 3x^2)}{x^{1/2}}$

$= 6x^{1/2} + 3x^2$

$\therefore p = 1/2, \quad q = 2$

6b. $\dfrac{dy}{dx} = 6x^{1/2} + 3x^2$

$y = \int 6x^{1/2} + 3x^2 \, dx$

$= \dfrac{6}{(3/2)} x^{3/2} + \dfrac{3}{3} x^3 + c$

$= 4x^{3/2} + x^3 + c$

$x = 4, \quad y = 90 \qquad \therefore \qquad 90 = 4(4)^{3/2} + 4^3 + c$

$90 = 32 + 64 + c$

$c = -6$

$\therefore \quad y = 4x^{3/2} + x^3 - 6$

7a. $F(x) = x^2 + (k+3)x + k$

$b^2 - 4ac : \quad (k+3)^2 - 4(1)(k)$
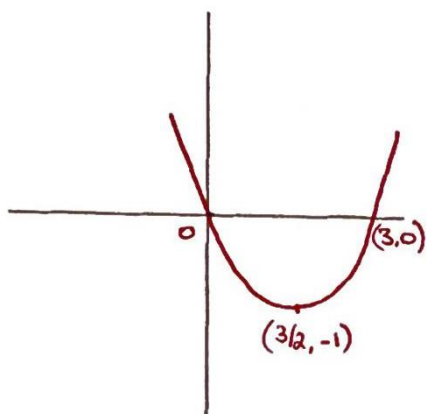
$k^2 + 6k + 9 - 4k$

$= k^2 - 2k + 9$

7b. $(k+1)^2 - 1 + 9$

$= (k+1)^2 + 8$

7c. $F(x)$ has real roots iff $b^2 - 4ac \geqslant 0$

$(k+1)^2 \geqslant 0 \; \forall \, k \implies b^2 - 4ac \geqslant 0 \quad \therefore \; F(x)$ has real roots $\forall \, k$

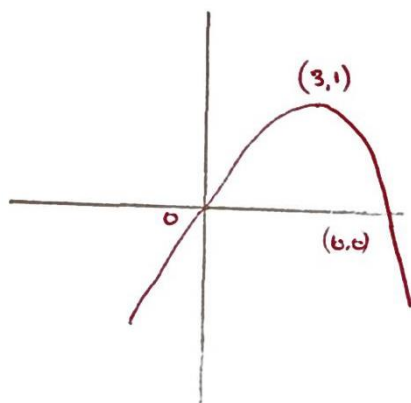**8a.**

$y = f(x) \rightarrow y = f(2x)$

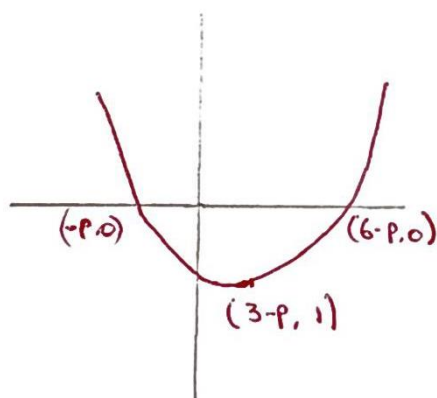stretch s.f. ½ in x direction

8b.

$y = f(x) \rightarrow y = -f(x)$

reflection in x axis

8c.

$y = f(x) \rightarrow y = f(x+a)$

translation left a units

9a.

$2 + 4 + 6 + \dots + 100$

how many terms?

$100 = 2 + (n-1)2$

$100 = 2 + 2n - 2$

$n = 50$

A.P. $a = 2 \quad d = 2$

$S_n = \frac{1}{2} n (a + \ell)$

$S_{50} = \frac{1}{2} (50)(2 + 100)$

$= 25 \times 102$

$= 2550$

9b: $k + 2k + 3k + \ldots + 100$

A.P. $\quad a = k \quad, \quad d = k$

$U_n = k + (n-1)k$

$100 = k + (n-1)k$

$100 = k + nk - k$

$n = \dfrac{100}{k}$

9b:ii.

$\begin{aligned} S_n &= \tfrac{1}{2}n(a + \ell) \\ &= \tfrac{1}{2} \cdot \dfrac{100}{k}(k + 100) \\ &= \dfrac{50k}{k} + \dfrac{5,000}{k} \\ &= 50 + \dfrac{5000}{k} \end{aligned}$

9c. $\quad 2k+1 \quad, \quad 4k+4, \quad 6k+7$

$a = 2k+1 \qquad d = 2k+3$

$\begin{aligned} U_{50} &= a + 49d \\ &= 2k+1 + 49(2k+3) \\ &= 2k+1 + 98k + \cancel{127}\ 147 \\ &= 100k + 148 \end{aligned}$

10a. $y = (x+1)(x+3)^2 \qquad$ root at $x = -1$

$\qquad\qquad\qquad\qquad\qquad$ double root at $x = -3$

when $x = 0 \qquad y = 1 \cdot 3^2 = 9$

10b.
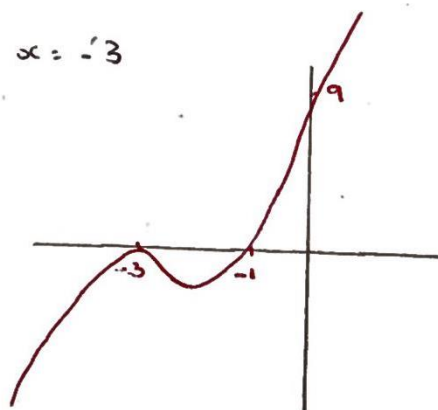
$$y = (x+1)(x+3)^2$$
$$= (x+1)(x^2+6x+9)$$
$$= x^3 + 6x^2 + 9x + x^2 + 6x + 9$$
$$= x^3 + 7x^2 + 15x + 9$$

$$\frac{dy}{dx} = 3x^2 + 14x + 15$$

10c.

when $x = -5$ $y = (-5+1)(-5+3)^2$
$$= -4(4)$$
$$= -16 \qquad A \quad (-5, -16)$$

$$\frac{dy}{dx} = 3(-5)^2 + 14(-5) + 15$$
$$= 75 - 70 + 15$$
$$= 20$$

$$y - -16 = 20(x - -5)$$
$$y + 16 = 20x + 100$$
$$y - 20x - 84 = 0$$
$$\therefore y = 20x + 84$$

10d.

Parallel $\therefore$ gradients are the same

$$\Rightarrow \frac{dy}{dx} = 20$$

$$3x^2 + 14x + 15 = 20$$
$$3x^2 + 14x - 5 = 0$$
$$(3x - 1)(x + 5) = 0$$
$$x = -5 \quad \text{or} \quad x = 1/3$$

$$\therefore \text{at} \quad B \quad x = 1/3$$