



**General Certificate of Education (A-level)  
June 2013**

**Mathematics**

**MS04**

**(Specification 6360)**

**Statistics 4**

**Final**

***Mark Scheme***

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## Key to mark scheme abbreviations

M	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
A	mark is dependent on M or m marks and is for accuracy
B	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation
✓ or ft or F	follow through from previous incorrect result
CAO	correct answer only
CSO	correct solution only
AWFW	anything which falls within
AWRT	anything which rounds to
ACF	any correct form
AG	answer given
SC	special case
OE	or equivalent
A2,1	2 or 1 (or 0) accuracy marks
-x EE	deduct $x$ marks for each error
NMS	no method shown
PI	possibly implied
SCA	substantially correct approach
c	candidate
sf	significant figure(s)
dp	decimal place(s)

### No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

**Otherwise we require evidence of a correct method for any marks to be awarded.**

Q	Solution	Marks	Total	Comments
<b>1(a)</b>	$s_1^2 = \frac{4.68}{12} = 0.39$ $s_2^2 = \frac{8.10}{9} = 0.9$	B1	1	Both
<b>(b)</b>	$H_0 : \sigma_X^2 = \sigma_Y^2$ $H_1 : \sigma_Y^2 > \sigma_X^2$ $F_{\text{calc}} = \frac{0.9}{0.39} = 2.31$ AWR $\nu_1 = 9, \nu_2 = 12$ $F_{\text{crit}} = 2.796$ Insufficient evidence to reject $H_0$ , so conclude that variability of heights is the same.	B1 M1A1 B1 B1		Both  Both; (df can be implied by correct CV).
	<b>Total</b>		<b>6</b>	
			<b>7</b>	
<b>2(a)</b>	$\frac{4}{p} = \frac{1-p}{p^2}$ $\Rightarrow 5p^2 = p \Rightarrow p = 0.2$ ( $p \neq 0$ )	M1A1 A1	3	
<b>(b)(i)</b>	$P(X > 7   X > 4) = \frac{0.8^7}{0.8^4}$ $= 0.512$	M1m1 A1	3	$0.8^3$ written down – using memory property is B2.
<b>(ii)</b>	$0.8^n < 0.0001$ or $1.25^n > 10000$ $\Rightarrow n > \frac{\log 10000}{\log 1.25}$ Least $n$ is 42.	M1 M1m1 A1	4	Answer from calculator B4 (CAO).
	<b>Total</b>		<b>10</b>	
<b>3(a)</b>	$\nu = 7$ CV = 1.415 $\frac{0.1625}{\left(\frac{s}{\sqrt{8}}\right)} = 1.415$ $\Rightarrow s = 0.3248$	B1 B1 M1A1 A1	5	(df can be implied by correct CV)  AWFW [1.415, 1.420]  Accept AFW [0.324, 0.325].
<b>(b)</b>	$\nu = 7 \Rightarrow CVs = 1.69, 16.01$ $\frac{0.3248\sqrt{7}}{\sqrt{16.01}} < \sigma < \frac{0.3248\sqrt{7}}{\sqrt{1.69}}$ $\Rightarrow (0.215, 0.661)$	B1B1 M1 A1✓ A1	5	(df can be implied by correct CV)  Or for interval in terms of variances. CAO ( <b>not</b> variances here.)
	<b>Total</b>		<b>10</b>	

Q	Solution	Marks	Total	Comments
4(a)	$1 - e^{-\frac{1}{\mu}x} = \frac{1}{4}, \quad \frac{3}{4}$ $Q_1 = \mu \ln\left(\frac{4}{3}\right)$ $Q_3 = \mu \ln 4$ $IQR = \mu \ln 3$	M1	5	Either.  M1 for attempting either $Q_1$ or $Q_3$ .  CAO
		M1A1		
		A1		
		A1		
(b)	$E(X^2) = \int_0^{\infty} \frac{1}{\mu} x^2 e^{-\frac{1}{\mu}x} dx$ $= \left[ -x^2 e^{-\frac{1}{\mu}x} \right]_0^{\infty} + \int_0^{\infty} 2x e^{-\frac{1}{\mu}x} dx$ $= 0 + 2\mu \cdot \mu = 2\mu^2 \quad (\text{AG})$	M1	4	Knowledge of formula.  Using integration by parts.
		M1A1		
		A1		
(c)	$SD = \sqrt{2\mu^2 - \mu^2} = \mu$  $\ln 3 > 1 \Rightarrow SD < IQR$	B1	3	
		M1A1		
<b>Total</b>			<b>12</b>	
5(a)	Normal distribution. Common variance.	E1 E1	2	
(b)	$H_0: \mu_m - \mu_e = 0 \quad H_1: \mu_m - \mu_e > 0$ $\bar{m} - \bar{e} = 25.5 - 18 = 7.5$ $s^2 = \frac{470 + 300}{10 + 8 - 2} = 48.125$ $\frac{7.5 - 0}{\sqrt{48.125(8^{-1} + 10^{-1})}} = 2.28$ $\nu = 16 \quad t_{\text{crit}} = 2.121$  Sufficient evidence at 2.5% level to reject $H_0$ and believe that morning journeys are longer, on average.	B1	9	Both  Accept [48.12,48.13] M1 requires a decent go at <b>both</b> numerator and denominator.  (df can be implied by correct CV)
		B1		
		M1A1		
		M1A1		
		B1B1		
<b>Total</b>			<b>11</b>	

Q	Solution	Marks	Total	Comments
6(a)	Mean = $\frac{220}{100} = 2.2$	B1	1	
(b)	19.67 10.81 4.76 2.49	M1 A2	3	–1 EE (no negative marks). Accept 19.66 and 10.82 from graphics calculator. Allow ‘1 – rest’ for 2.49, if implied by correct following working.
(c)	$H_0$ : Po(2.2) is a suitable model. (OE)	B1		2.2. not required. Cf. qn re Gwyneth’s belief.
	Combine last two classes.	M1		Expected frequencies below 5.
	$\chi^2_{\text{calc}} = 3.58$ to 3.61	M1A1		AWFW
	$\nu = 6 - 2 = 4$	B1		(df can be implied by correct CV)
	$\chi^2_{\text{crit}} = 7.779$	B1		
	Retain $H_0$ : Po(2.2) is a suitable model. (OE)	E1✓	7	2.2. not required. Cf. qn re Gwyneth’s belief
	(OE) $\equiv$ a statement about Gwyneth’s belief. Cf Qn.			
<b>Total</b>			<b>11</b>	
7(a)(i)	$E\left(\frac{3R}{2}\right) = \frac{3}{2}E(R)$ $= \int_0^\gamma \frac{3r^2}{\gamma^2} du = \left[\frac{r^3}{\gamma^2}\right]_0^\gamma$ $= \gamma$	M1 M1A1 A1	4	
(ii)	$\text{Var}\left(\frac{3R}{2}\right) = \frac{9}{4} \times \frac{\gamma^2}{18} = \frac{\gamma^2}{8}$	M1A1	2	
(b)(i)	$E(kT) = \gamma \Rightarrow \frac{3k}{4}\gamma = \gamma \Rightarrow k = \frac{4}{3}$	M1A1	2	
(ii)	$\text{Var}\left(\frac{4}{3}T\right) = \frac{16}{9}\text{Var}(T) = \frac{16}{9} \times \frac{3}{16}\gamma^2 = \frac{\gamma^2}{3}$	M1A1		
	$\text{RE}\left(\frac{3}{2}R \text{ wrt } \frac{4}{3}T\right) = \frac{\text{Var}\left(\frac{4}{3}T\right)}{\text{Var}\left(\frac{3}{2}R\right)} = \frac{\gamma^2}{3} \times \frac{8}{\gamma^2} = \frac{8}{3}$	M1A1	4	
(iii)	Since this is greater than 1, prefer $\frac{3}{2}R$ .	M1A1	2	Allow ‘because $\frac{3}{2}R$ has the smaller variance’. Award M1 for comparing <b>their</b> RE with 1, or comparing variances. A1 is CSO and requires the previous A marks.
<b>Total</b>			<b>14</b>	
<b>TOTAL</b>			<b>75</b>	