

Parallel and Perpendicular Lines Mark Scheme		
<b>1(a)</b>	Parallel lines have the same gradient ( <i>m</i> value in $y = mx + c$ )	[1]
<b>1(b)</b>	Perpendicular lines meet at $90^\circ$ ( <i>their gradients multiply to give</i> $-1$ )	[1]
<b>2(a)</b>	$y - 5x = 2$	[1]
<b>2(b)</b>	$2y = 6x + 10$	[1]
<b>3(a)</b>	$y = -3x + 2$	[1]
<b>3(b)</b>	$y = 4x - 3$	[1]
<b>3(c)</b>	$y = 2x - 7$	[1]
<b>4(a)</b>	No	[1]
<b>4(b)</b>	No	[1]
<b>4(c)</b>	Yes	[1]
<b>4(d)</b>	Yes	[1]
<b>4(e)</b>	No	[1]
<b>5(a)</b>	$m = \frac{\text{change in } y}{\text{change in } x} = \frac{7 - 1}{10 - -2} = \frac{6}{12} = \frac{1}{2}$	[1] Calculating gradient
	$7 = \frac{1}{2} \times 10 + c ; 7 = 5 + c ; c = 2$ $1 = \frac{1}{2} \times (-2) + c ; 1 = -1 + c ; c = 2$ $y = \frac{1}{2} x + 2$	[1] Substituting values for $x$ and $y$ to find the equation
<b>5(b)</b>	Perpendicular	[1]
<b>5(c)</b>	Parallel	[1]
<b>5(d)</b>	Parallel	[1]
<b>5(e)</b>	Neither	[1]
<b>5(f)</b>	Neither	[1]
<b>5(g)</b>	Perpendicular	[1]

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<b>6</b>	Parallel lines have the same gradient, so Gradient of D = Gradient of C	[1] Parallel lines define by equal gradient
	$Gradient\ of\ C = \frac{change\ in\ y}{change\ in\ x} = \frac{4 - -2}{11 - 2} = \frac{6}{9} = \frac{2}{3}$	[1] Calculation
	$Gradient\ of\ D = \frac{2}{3}$	[1] Correct gradient
	Points on D = $(3 + n, 2 + \frac{2}{3}n)$ Point on D (6,4)	[1] accept any correct point on D
<b>7(a)</b>	$Gradient = \frac{3}{2}$	[1] Correct gradient
	$y = \frac{3}{2}x - 1$	[1] Correct equation of the line
<b>7(b)</b>	$Gradient = -\frac{2}{3}$	[1] Correct gradient
	$y = -\frac{2}{3}x + 1$	[1] Correct equation of the line
<b>8(a)</b>	$Gradient\ of\ A = \frac{change\ in\ y}{change\ in\ x} = \frac{1}{2}$	[1] Correct gradient
	$y = \frac{1}{2}x$	[1] Correct equation of the line
	$Gradient\ of\ B = \frac{change\ in\ y}{change\ in\ x} = -2$	[1] Correct gradient
	$y = -2x + 5$	[1] Correct equation of the line
<b>8(b)</b>	The product of gradients for perpendicular lines is -1	[1] Definition of perpendicular gradient
<b>9(a)</b>	Parallel so $m = 1/3$	[1] for correctly determining the gradient
	Substituting vales for x and y $14 = \frac{1}{3} \times 9 + c ; c = 11. ; y = \frac{1}{3}x + 11$	[1] for calculating c
<b>9(b)</b>	Perpendicular so $m \times -3 = -1 ; m = \frac{-1}{-3} ; m = \frac{1}{3}$	[1] for correctly determining the gradient
	Substituting vales for x and y $4 = \frac{1}{3} \times 5 + c. ; c = \frac{7}{3} . ; y = \frac{1}{3}x + \frac{7}{3}$	[1] for calculating c
<b>9(c)</b>	Perpendicular so $m \times \frac{1}{3} = -1. ; m = -1 \times 3$ $m = -3$	[1] for correctly determining the gradient
	Substituting vales for x and y $-5 = -3 \times -1 + c ; c = -8 ; y = -3x - 8$	[1] for calculating c

Turn over ►

<b>9(d)</b>	$2y = 3(2 - 3x) ; 2y = 7 - 9x ; y = -\frac{9}{2}x + \frac{7}{2}$ Line is parallel, so $m = -\frac{9}{2}$	[1] for correctly determining the gradient
	$y = x + 8$ and $y = -3x + 4$ $x + 8 = -3x + 4 ; 4x + 8 = 4 ; 4x = -4 ; x = -1$  $y = -1 + 8 ; y = 7$ <i>Passes through the point (-1,7)</i>	[1] for finding the intersection point
	$y = -\frac{9}{2}x + c ; 7 = -\frac{9}{2} \times -1 = c ; c = \frac{5}{2}$ $y = -\frac{9}{2}x + \frac{5}{2}$	[1] for calculating c
<b>10</b>	Opposite side of rectangle has the same gradient $y = \frac{2}{3}x + c$	[1] Value of c could be anything except 3.
	Other sides of rectangle must meet these two sides at $90^\circ$ , so are perpendicular and have gradients such that they multiply with the original sides to make $-1$ . $\frac{2}{3} \times -\frac{3}{2} = -1 ; m = -\frac{3}{2}$	[1] Gradient of other two sides
	<i>Equation of lines must be:</i> $y = -\frac{3}{2}x + c$	[1] Where the two intercepts (c's) aren't equal.
<b>11(a)</b>	<i>Line A:</i> $5y - 2x - 2 = 0 ; 5y = 2x + 2 ; y = \frac{2}{5}x + \frac{2}{5}$ Line B is perpendicular, so the gradient is: $m \times \frac{2}{5} = -1 ; m = -\frac{5}{2}$ Equation of Line B $y = -\frac{5}{2}x + c ; -1 = -\frac{5}{2} \times 1 + c ; c = \frac{3}{2} ; y = -\frac{5}{2}x + \frac{3}{2}$	[1] Find line B
	$y = \frac{2}{5}x + \frac{2}{5} , y = -\frac{5}{2}x + \frac{3}{2} ;$ $\frac{29}{10}x = \frac{11}{10} ; 29x = 11 , x = \frac{11}{29}$  Substituting this value back in to find y $y = -\frac{5}{2}x + \frac{3}{2} ; y = -\frac{5}{2} \times \frac{11}{29} + \frac{3}{2} ; y = -\frac{55}{58} + \frac{3}{2}$  $y = \frac{16}{29}$ <i>Point of intersection is <math>(\frac{11}{29}, \frac{16}{29})</math></i>	[1] Find the point of intersection by solving as simultaneous equations
<b>11(b)</b>	A third line, C, is perpendicular to B and has y-intercept of -3. Write down the equation of C.  Has the same gradient as A , $m = \frac{2}{5}$ Has a y-intercept of -3. , $c = -3$ $y = \frac{2}{5}x - 3$	[1] Equation of line C

END