

Vectors Mark Scheme		
1(a)	$2\mathbf{a} + \mathbf{b}$	[1] Vector representing M to L
1(b)	$\frac{1}{2}(2\mathbf{a} + \mathbf{b}) = \mathbf{a} + \frac{\mathbf{b}}{2}$	[1] Vector representing M to P
1(c)	$4 \begin{bmatrix} \mathbf{a} \\ \mathbf{b}/2 \end{bmatrix} = \begin{bmatrix} 4\mathbf{a} \\ 2\mathbf{b} \end{bmatrix} = 2 \begin{bmatrix} 2\mathbf{a} \\ \mathbf{b} \end{bmatrix} = 2 \overrightarrow{ML}$	[1] Vector representing M to N
2	$\overrightarrow{GF} = 3\mathbf{a} - \mathbf{a} + 5\mathbf{b} + 4\mathbf{b}$	[1] Vector representing G to F which is the sum of G to E and E to F
	$\overrightarrow{GF} = 2\mathbf{a} + 9\mathbf{b}$	[1] Vector representing G to F
	$\overrightarrow{GH} = 3(2\mathbf{a} + 9\mathbf{b}) = 6\mathbf{a} + 27\mathbf{b}$	[1] Vector representing G to H which is 3 times G to F
3	$\overrightarrow{FC} = \frac{\mathbf{a}}{2}$	[1] Vector representing F to C
	$\overrightarrow{BE} = \frac{3}{4}\mathbf{a}$	[1] Vector representing B to E
	$\overrightarrow{FE} = \frac{5}{4}\mathbf{a} - \mathbf{b}$	[1] $\overrightarrow{FE} = \overrightarrow{FC} + \overrightarrow{CB} + \overrightarrow{BE}$
4(a)	$\overrightarrow{LM} = -2\mathbf{a}, \quad \overrightarrow{MN} = 2\mathbf{a} + 2\mathbf{b}, \quad \overrightarrow{NK} = 3\mathbf{a} + \mathbf{b}.$	[1] $\overrightarrow{LK} = \overrightarrow{LM} + \overrightarrow{MN} + \overrightarrow{NK}$
	$\overrightarrow{LK} = -2\mathbf{a} + 2\mathbf{a} + 2\mathbf{b} + 3\mathbf{a} + \mathbf{b}$ $\overrightarrow{LK} = 3\mathbf{a} + 3\mathbf{b}$	[1] Vector representing L to K in its simplest form
4(b)	$\overrightarrow{LP} = \frac{1}{3}(3\mathbf{a} + 3\mathbf{b})$	[1] Vector representing L to P
	$\overrightarrow{LP} = \mathbf{a} + \mathbf{b}$	[1] Simplifying
	$\overrightarrow{MP} = \overrightarrow{ML} + \overrightarrow{LP} = 2\mathbf{a} + \mathbf{a} + \mathbf{b}$	[1] Vector representing M to P
	$\overrightarrow{MP} = 3\mathbf{a} + \mathbf{b} = \overrightarrow{NK}$	[1] Showing M to P is the same as N to K
5(a)	$-\mathbf{a} + \mathbf{b}$	[1] Vector representing B to C
5(b)	$-2\mathbf{a}$	[1] Vector representing D to E
5(c)	$-2\mathbf{a} + \mathbf{b}$	[1] Vector representing D to E
5(d)	$\mathbf{a} + \mathbf{b}$	[1] Vector representing D to E

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6	$\overrightarrow{DA} = 4\mathbf{b}$	[1] Magnitude of 4
	$\overrightarrow{BE} = 2\mathbf{a}$	[1] Vector representing B to E
	$\therefore \overrightarrow{AE} = 5\mathbf{a}$	[1] Vector representing A to E
	$\overrightarrow{DE} = 4\mathbf{b} + 5\mathbf{a}$	[1] Vector representing D to E
7(a)	$-\mathbf{a} + \mathbf{b}$	[1] Vector representing B to C
7(b)	$\overrightarrow{AC} = \overrightarrow{CE} = \mathbf{b}$	[1] Vector representing C to E
	$\overrightarrow{DE} = \frac{1}{4}\overrightarrow{CE} = \frac{1}{4}\mathbf{b}$	[1] Vector representing D to E
	$\overrightarrow{CD} = \overrightarrow{CE} - \overrightarrow{DE} = \mathbf{b} - \frac{1}{4}\mathbf{b} = \frac{3}{4}\mathbf{b}$	[1] Vector representing C to D
	$\overrightarrow{DB} = \overrightarrow{DC} + \overrightarrow{CB} = -\frac{3}{4}\mathbf{b} - \mathbf{b} + \mathbf{a} = -\frac{7}{4}\mathbf{b} + \mathbf{a}$	[1] Vector representing D to B
8	$\overrightarrow{BC} = -2\mathbf{a} + 3\mathbf{b}$	[1] Vector representing B to C
	$\overrightarrow{BD} = -\frac{\mathbf{a}}{2} + \frac{3}{4}\mathbf{b}$	[1] Vector representing B to D
	$\overrightarrow{AD} = 2\mathbf{a} - \frac{\mathbf{a}}{2} + \frac{3}{4}\mathbf{b} = \frac{3}{2}\mathbf{a} + \frac{3}{4}\mathbf{b}$	[1] Vector representing A to D
	$\overrightarrow{AE} = \frac{1}{2}\left(\frac{3}{2}\mathbf{a} + \frac{3}{4}\mathbf{b}\right)$	[1] Vector representing A to E
	$= \frac{3}{4}\mathbf{a} + \frac{3}{8}\mathbf{b} = \frac{3}{4}\left(\mathbf{a} + \frac{\mathbf{b}}{2}\right)$	[1] Simplification not required

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9(a)	$2a - 3b$	[1] $\overrightarrow{DC} = \overrightarrow{DA} + \overrightarrow{AC}$
9(b)	$AD:BE:CF = 3:2:2$ $AD:BE:CF = 3b:2b:2b$ $CF = 2b$	[1] Ratio finds $\overrightarrow{FC}$
	$\overrightarrow{FD} = \overrightarrow{FC} + \overrightarrow{CB} + \overrightarrow{BA} + \overrightarrow{AD}$ $= -2b - a - a + 3b$ $= -2a + b$	[1] Final answer
9(c)	$\overrightarrow{DE} = -3b + a + 2b$ $= a - b$	[1] Vector representing D to E
	$\overrightarrow{EX} = x\overrightarrow{DE}$ <i>Need 1 lot of <math>\overrightarrow{EX}</math> to reach CF, and gives:</i> $\overrightarrow{CX} = \overrightarrow{XF} = b$	[1] Comparison
	$CX:XF = 1:1$	[1] Correct Ratio
10	$\overrightarrow{AD}:\overrightarrow{DY}:\overrightarrow{YC} = 1:1:1$ $\overrightarrow{AD} = \overrightarrow{DY} = \overrightarrow{YC} = a$ $\overrightarrow{BC} = \overrightarrow{BD} + \overrightarrow{DY} + \overrightarrow{YC}$ $= -(3b - a) + a + a$ $= a - 3b + a + a$ $= 3a - 3b$ $= 3(a - b)$	[1] Find vector B to C
	$\overrightarrow{AB} = \overrightarrow{AD} + \overrightarrow{DB}$ $= a + 3b - a$ $= 3b$ $\overrightarrow{AX}:\overrightarrow{XB} = 2:1$ $\overrightarrow{AX} = 2b$	[1] Find vector A to X
	$\overrightarrow{XY} = \overrightarrow{XA} + \overrightarrow{AD} + \overrightarrow{DY} = -2b + a + a$ $= 2a - 2b$ $= 2(a - b)$ <i>BC is a multiply of XY, so they are going in the same direction</i>	[1] Find vector X to Y

END